Math 583B		Research in Ge etric na sis					rinų	<b>5</b>
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Here are some observations about the writing of mathematics that I ho e wi be usefu as \_ou word on the writing assignment for this course

**G** as an a ience  $\measuredangle$  s with an written iece mathematica e osition must be written with a articu ar au ience an s eci c goas in min  $\dashv$  e sure ou have a c ear sense of what these are before ou start writing

f here r cess. It is important to bear in mine that writing is a *process* ust if erroring a theorem time the\_sit own to write ust as no one ro uces a comete we structure roof the rst time the, thin about a rob em ost goo e ositor, rose has been thorough. rewritten at east once or twice before it reaches the rea er with *i*e, sections un ergoing erha s three to ve ma or revisions o some eo e this thought majes the ros ect of writing seem aunting or even overwhe ming but it nee n t he i ea that much of what ou write wi eventua be re ace or iscar e can be iberating Just sit own an write *i* nowing that an thing that oesn't measure u can ater be e **o** might we n \_ourse f throwing awa, the rst severa ages \_ou write this is not waste time since the tria an error rocess he s\_ou immense\_ in c arif\_ing what \_ou rea \_ want to sa\_

hen \_ou begin writing a raft the intro uction ma\_ not be the best ace to start since the structure of the a er ma\_ not become com ete\_ c ear unti ater in the rocess  $r_{-}$ starting somewhere in the mi e with whichever art of the a er is c earest in \_our min s soon as \_ou have a section or more in reative \_ coherent form sit bac\_ an rea it ut \_ourse f in the min of \_our au ience an see if it mages com ete sense hen rewrite

hen \_ou have something \_ou thing is c ose to acce table give it to someone e se to rea an comment on hen rewrite again

fter ou thing the a er is nishe go through it with a ne toothe comb an a shar ra or har en our e nitions statements of theorems an roofs arif, our ogic an our intuitive escritions age sure our s e ing unctuation an grammar are absoute, correct mit nee ess wor s termino og, an s\_mbo s

Ote that rewriting usua means much more than sim correcting errors. It means oof ing critica at what ou ve written both oca an goba guring out what worfs we an what oesn't an oing whatever is necessar, to make the whoe thing worf erfect.

**n\_jenti ns** though \_ou might not be ieve it after rea ing some of the mathematica writing that has ma e it into rint mathematica writing shou fo ow the same conventions of grammar usage unctuation an s e ing as an\_other writing his means in articular that \_ou must write comete sentences organile into aragra hs hieman\_mathematica terms have technica meanings that are i\_erent from their usage in or inar\_ng ish \_ou shou stills be careful to observe the usual rules regaring arts of s eech an subject, verb agreement though \_ou will run across \_a too man\_mathematicians who write ungrammatica sentences if e\_u ose f is an onto ma \_ don't you do it!

If \_ou are not a native ng ish s easer it wou be a goo i ea to cu tivate the habit of assing a native s easer to oos over \_our writing before \_ou submit it

recisi n<br/>  ${\cal A}$  In mathematica writing more than an<br/>, other fin ~ recision is of ~ aramount

correct\_use he sentence\_tet f be the function whose value at a larticular number is equal to the square of that number a le to the number itse f lis far less clear than tet f be the function e ne b.  $f_{-x}$  is  $x^2$  is not the other han electric clear that is use as obscure less that the term is that is use as obscure less that term is use as obscure less that term is use as obscure less term is that is use as obscure less term is that term is use that term is use as obscure less term is that term is use as obscure term is that term is use as obscure term is that term is use as obscure term is that term is use term is that term is use term is that term is that term is use term is that term is use term is that term is use term is that term is term is used as obscure term is that term is term is term is that term is term is term is term is term is term.

Here are some gui e ines for using mathematica s\_mbo s in \_our writing

• ee the number of name s\_mbos to the minimum necessar\_ for c arit\_ I ea \_ each s\_mbo shou refer to an ob ect whose roe in the a er or in a articu ar section of the a er is im ortant enough that \_ou want the rea er to remember it b\_ name \_ his is es ecia \_ true in statements of theorems \_ hich of the fo owing statements is c earer

 $\Box$  he re If G is any Lie group, there exists a Lie group  $\tilde{G}$  that is the universal covering group of G.

- The re ' Every Lie group has a universal covering group.
- f course even if ou use the secon version in the roof of the theorem ou wi robab , want to intro uce s\_mbo s such as G an  $\tilde{G}$  to refer to the given grou an its universa cover
- ing e s\_mbo s an short sim e formu as shou be inc u e right in \_our ara, gra hs but a formu a that is arge or es ecia \_ im ortant shou be centere on a ine b\_ itse f \_this is ca e a\_ is a\_e formu a
- ver\_mathematica s\_mbo or formu a whether inc u e in the te t or is a\_e must have a e nite grammatica function in a sentence usua \_ as a noun or a c ause \_ onsi er the fo owing sentence

If x > we see that  $x^2 - x$  must be greater than

Here the formula, x > - is a clause whose verb is x > - while  $x^2 - x$  functions as a noun

- If a is a e formu a en s a sentence it must be fo owe b a erio
- he best wa\_ to ensure that \_our formu as function grammatica \_ correct \_ is to rea each sentence a ou hen \_ou o so bear in min\_that man\_s\_mbo s can be rea in severa i\_erent wa\_s for e am e the s\_mbo / can be rea as equa s equa to \_ be equa to \_ or is equa to \_ e en ing on conte t
- equa to be equa to or is equa to e en ing on conte t mbo s re resenting mathematica re ations \_ife > or  $\in$  or o erators \_ife – or  $\cap$  shou be use on to connect other mathematica s mbo s not wor s or e am e o *not* write

that is  $\in T_x M$ 

Instea this sentence cou be rewritten as fo ows

t et  $\boldsymbol{a} \in T_x M$  be a vector such that  $|\boldsymbol{a}| < 1$ 

• ractions an fractiona e ressions incu e in the tet shou be written with a s ash as in x/-g. If a fraction is so arge or commicate that it nees to be written using a hori onta bar it shou be is a e he on e ce tions are sma numerical fractions such as  $\frac{1}{2}$  which can be incu e in tet as ong as the.

• he s\_mbo s of s\_mbo ic ogic such as  $\exists \forall \land \lor \neg$  an  $\Rightarrow$  shou never be use in forma mathematica writing un ess \_ou are writing about s\_mbo ic ogic an the\_ a ear in ogica formu as therwise write out the wor s instea

itin s rces hen ou write a mathematics a er ou must ist in our bib iograh ever, ub ishe source from which ou obtain i eas mathematica resu ts roofs facts or s eci c anguage henever ou write something that ou obtaine from such a source ou must refer s eci ca to the source in the tet If ou use a arge amount of materia from one source as ou might o in an e ositor, a er it s ermissible to write something if e a of the resu ts in this section are from the tet material from but it s not enough ust to ist a a er or bood in our bib iograh. Here are some e am es of situations that require citations

 $\label{eq:he} \begin{array}{cccc} \mathbf{he} & \mathbf{i} & \mathbf{irra} & \mathbf{h} & \measuredangle & \mathrm{he} & \mathrm{conventions} & \mathrm{for} & \mathrm{bib} & \mathrm{iogra} & \mathrm{hic} & \mathrm{references} & \mathrm{in} & \mathrm{mathematica} & \mathrm{writing} \\ \mathrm{are} & \mathrm{somewhat} & \mathbf{i} & \mathrm{erent} & \mathrm{from} & \mathrm{those} & \mathrm{in} & \mathrm{other} & \mathrm{e} & \mathrm{s} & \mathrm{sam} & \mathrm{e} & \mathrm{bib} & \mathrm{iogra} & \mathrm{h} & \mathrm{is} & \mathrm{shown} & \mathrm{be} & \mathrm{ow} \\ \mathrm{the} & \mathrm{rst} & \mathrm{entr} & \mathrm{is} & \mathrm{for} & \mathrm{a} & \mathrm{boos} & \mathrm{the} & \mathrm{secon} & \mathrm{is} & \mathrm{for} & \mathrm{an} & \mathrm{un} & \mathrm{ub} & \mathrm{ishe} & \mathrm{re} & \mathrm{rint} & \mathrm{in} & \mathrm{an} & \mathrm{on} & \mathrm{ine} & \mathrm{atabase} \end{array}$ 

- [1] J. R. Dieudonné, P. R. Halmos, M. M. Schi er, and N. E. Steenrod, *How to write mathematics*, American Mathematical Society, Providence, 1981. Look especially at the essay by Halmos, which is a classic.
- [2] L. Gillman, Writing Mathematics Well, Mathematical Association of America, 1987.
- [3] D. E. Knuth, T. Larrabee, and P. M. Roberts, *Mathematical Writing*, Mathematical Association of America, Washington, 1989. Look especially at pages 1-8.