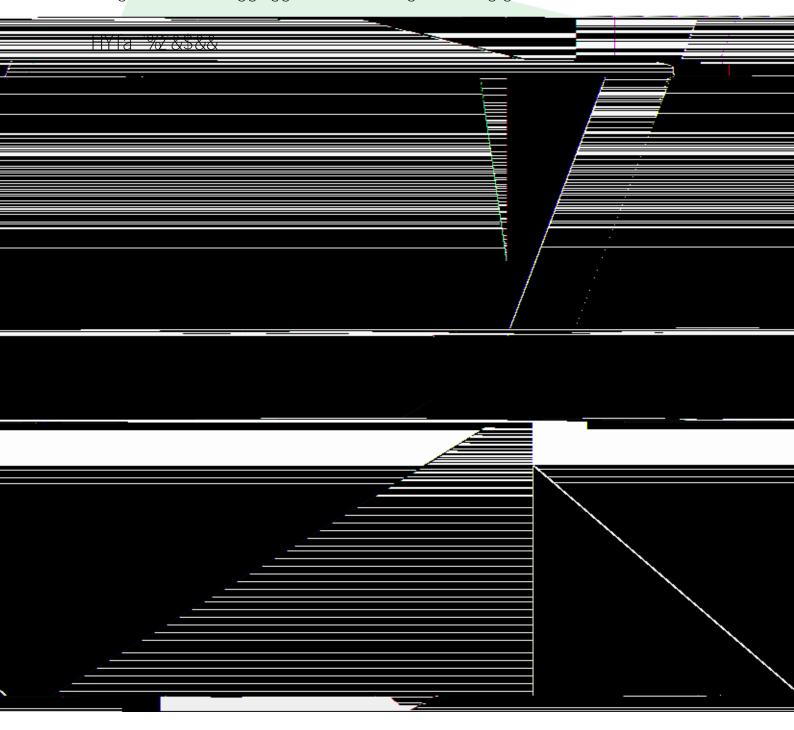


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fŽ*%%&£'-',) " %+- '-1 BGK 'Gh Xm5VfcUX'UbX'1 BGK '91 WXUb[Y'fZcf']bVci bX'gh XYbhg£'

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H\Y'hk c'ei]nnYg'k]``VY'\Y`X']b'K YY_'('UbX'K YY_'%\$žXi f]b['k cf_g\cd'h]a Yg''

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GhUfh'XUhY. K YY_&

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GhUfhXUhY. K YY_**

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8i Y'XUhY. '%#\$(#&\$&&`\$, .\$\$'DA

H\]g`]g`Ub`]bX]j]Xi U``Ugg][ba Ybhk\YfY`ghi XYbhg`k]```Udd`m`g_]``g``YUfbh`]b`h\Y`Wti fgY`hc`XYhYfa]bY`h\Y`f]g_cZU`dUfh]W``Uf`Ybj]fcba YbhU``WtbhUa]bUbh'`H\Y`UggYgga YbhYbWti fU[Yg`UbU`mh]WU``UbX`Wf]h]WU``h\]b_]b[UbX`WfYUh]j Y`dfcV`Ya `gc`j]b[`ig]b[`]bXi ghfm[i]XY`]bYg"

H\]g`Ugg][ba Ybh]g`gi Va]h\X`h\fci [\'Hi fb]h]b`UbX`ghi XYbhg`Xc`bchgYY`Hi fb]h]b`g]a]`Uf]hmfYdcfhg"

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H\]g Ugg][ba Ybh]g gi Va]h\X h\fci [\ Hi fb]h]b UbX gh XYbhg Xc bchgYY Hi fb]h]b g]a]\Uf]hmfYdcfhg"

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5 a Uf_'cZUh`YUgh'(\$i ']b'h\Y'ZbU`YI Ua]bUh]cb']g'fYei]fYX'VYZcfY'h\Y'WUgg'k cf_']g']bWi XYX']b'h\Y'ZbU`a Uf_'''H\YfYZcfYž'U'a Uf_'cZUh`YUgh'(\$i ']b'h\Y'ZbU`YI Ua]bUh]cb']g'fYei]fYX'hc'dUgg'h\Y'k \c`Y'Wci fgY''

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- <u>? Ymil_BGK_'8 UhYg</u>'! 'Y["'7 Ybgi g'8 UhYž'Yl Ua 'XUhYgž``UghXUmhc'Xfcd'U'Wci fgY'k]h\ci h_UWUXYa]\#]bUbW]U```]UV]`]hmYhW''
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